

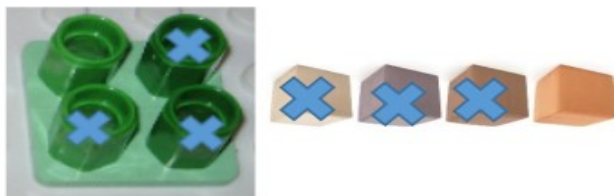
Subtraction

Key language which should be used: take away, less than, the difference, subtract, minus, fewer, decrease, '7 take away 3, the difference is four

Concrete

Physically taking away and removing objects from a whole (use various objects too) rather than crossing out children will physically remove the objects

$$4 - 3 = 1$$



Pictorial

Children to draw the concrete resources they are using and cross out.



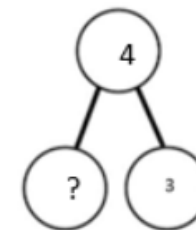
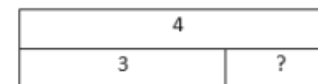
Use of the bar model.



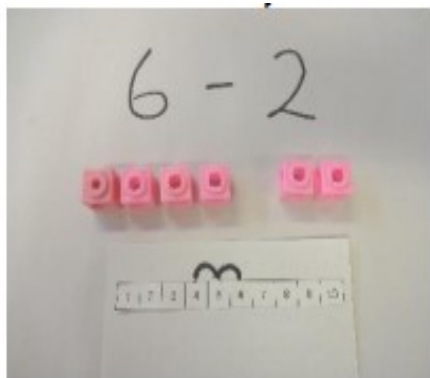
Abstract

$$4 - 3 =$$

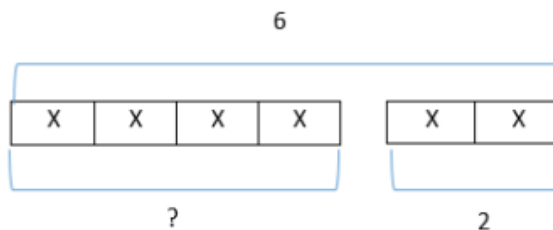
$$\square = 4 - 3$$



Counting back (using number lines or number tracks)

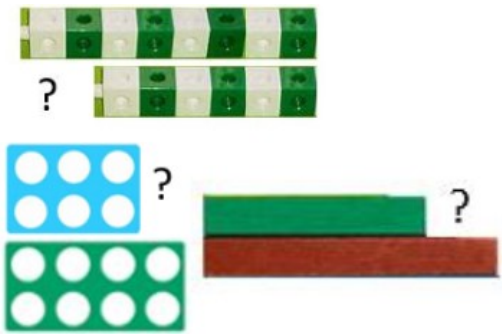


Children to represent what they see pictorially e.g.

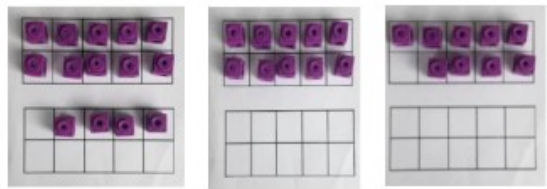


Concrete

Finding the difference (using cubes, numicon or Cuisenaire rods, other objects can also be used)



Making 10 (using numicon or ten frames)
14 - 5



Children could also do this by subtracting a 5 from the 10.

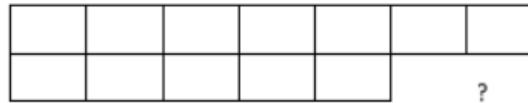


Pictorial

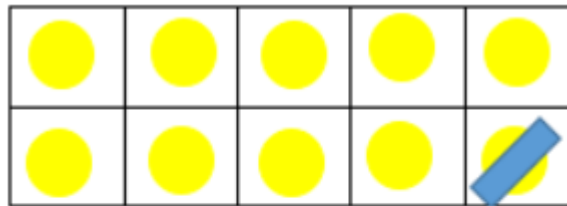
Children to draw the cubes/other concrete objects which they have used

XXXXXXXXX
XXXXXX

Use of the bar model



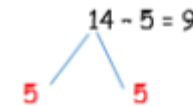
Children to present the ten frame pictorially



Abstract

Find the difference between 8 and 6.
8 - 6, the difference is ?
Children to also explore why
9 - 7 = 8 - 6 (the difference, of each digit, has changed by 1 do the difference is the same- this will help when solving 10000-9987)

14 - 5 = 9 You also want children to see related facts e.g. 15 - 9 = 5
Children to represent how they have solved it e.g.



14 is made up of 5, 5 and 4 so I can subtract one 5 to be left with 4 and 5



5 is made up of 4 and 1 so I can subtract 4 to make 10 and then 1 to get to 9

Concrete

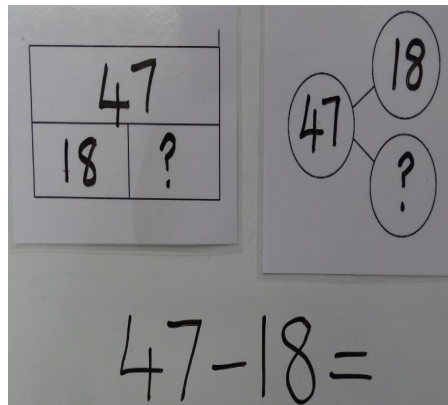
Pictorial

Abstract

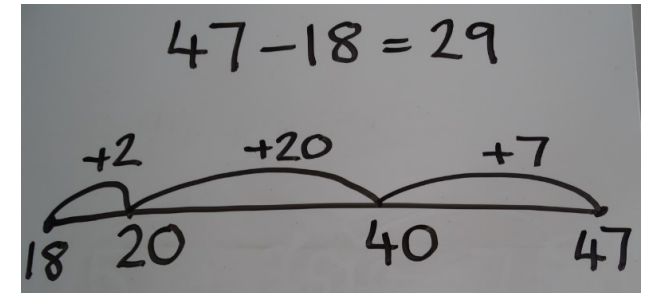
Counting on using a number line



Bar model

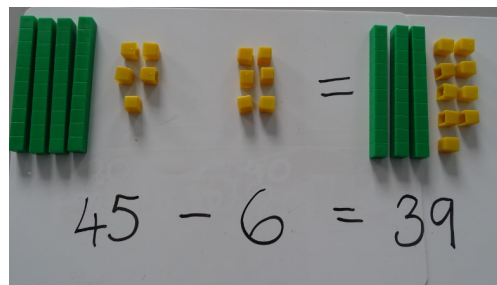
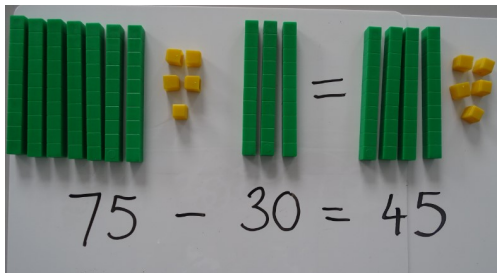


Abstract number line

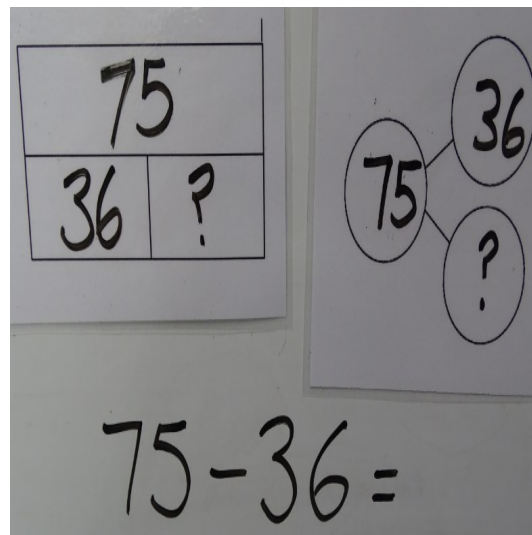


TO -TO using Dienes. Use partitioning and bridging 10.

75 - 36



Bar model



Children to start with the largest number and subtract the tens and then the ones.

75 - 36

75 - 30 = 45

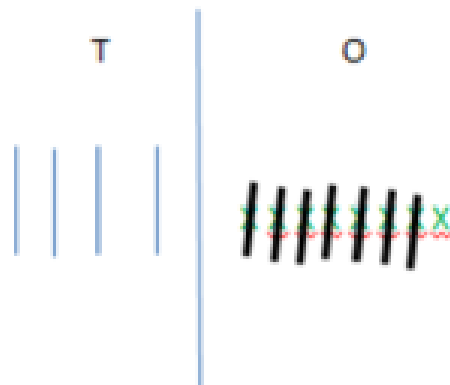
45 - 6 = 39

Concrete

Column method (using Dienes and no exchanging)
48-7



Pictorial



Abstract

Expanded and formal written method

$$\begin{array}{r} \text{T} \quad \text{O} \\ 40 \quad 8 \\ - 0 \quad 7 \\ \hline 40 \quad 1 \end{array}$$

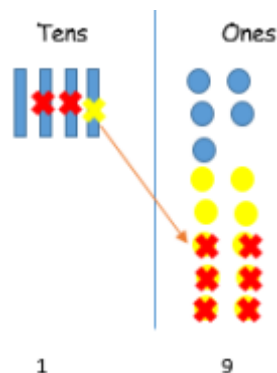
	4	8
-		7
	4	1

Column method (using Dienes and having to exchange)
45-26



- 1) Start by partitioning 10
- 2) Exchange one ten for ten more ones
- 3) Subtract the ones, then the tens.

Represent the Dienes pictorially



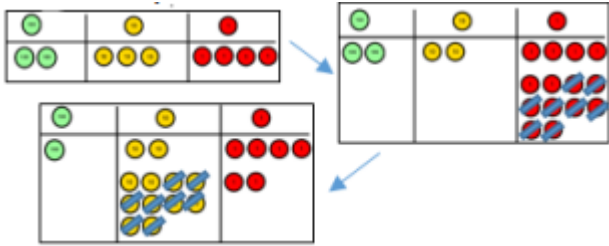
It's crucial that the children understand that when they have exchanged the 10 they still have 45. $45 = 30 + 15$

$$\begin{array}{r} \text{T} \quad \text{O} \\ \overset{30}{40} \quad 15 \\ - 20 \quad 6 \\ \hline 10 \quad 9 \end{array}$$

	4	5
-	2	6
	1	9

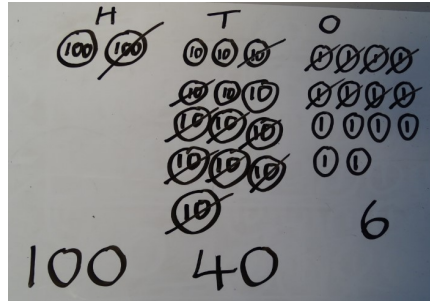
Concrete

Column method (using place value counters)
234-88

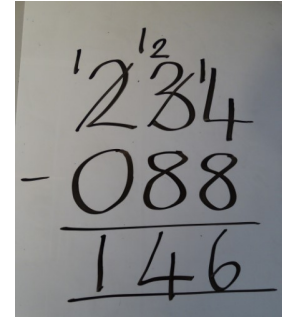
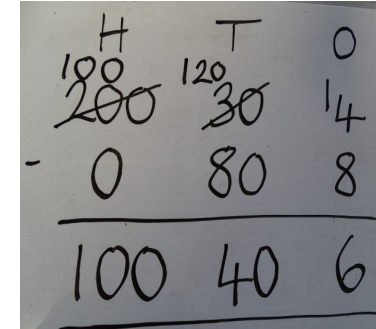


Pictorial

Once the children have had practice with the concrete, they should be able to apply it to any subtraction. Like the other pictorial representations, children to represent the counters.



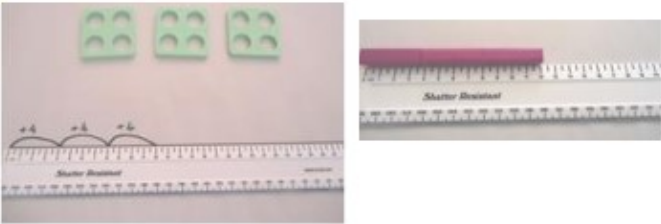

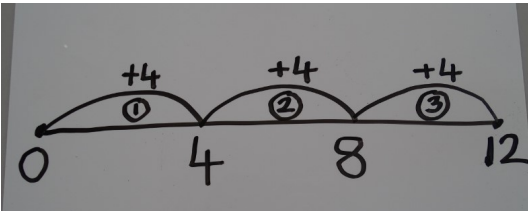


Abstract



Multiplication

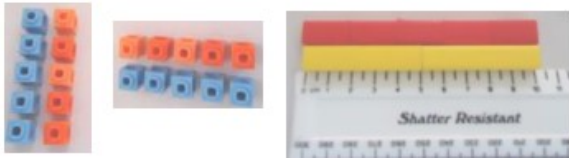
Key language which should be used: double, times, multiplied by, the product of, groups of, lots of, 'is equal to' 'is the same as', array, multiple, repeated addition, commutative.

Concrete	Pictorial	Abstract
<p>Repeated grouping/repeated addition (does not have to be restricted to cubes) 3 x 4 or 3 lots of 4</p> 	<p>Children to represent the practical resources in a picture e.g.</p> <p>XX XX XX XX XX XX</p> <p>Use of a bar model for a more structured method.</p> 	<p>3×4 $4 + 4 + 4$</p>
<p>Use number lines to show repeated groups- 3 x 4</p> 	<p>Represent this pictorially alongside a number line e.g:</p> 	<p>Abstract number line $3 \times 4 = 12$</p> 

Concrete

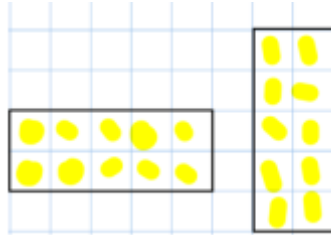
Use arrays to illustrate commutativity (counters and other objects can also be used)

$$2 \times 5 = 5 \times 2$$



Pictorial

Children to draw the arrays (draw round numicon)



Abstract

Children to be able to use an array to write a range of calculations e.g.

$$2 \times 5 = 10$$

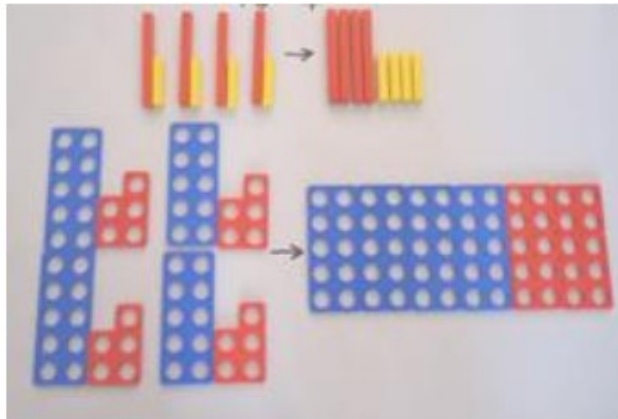
$$5 \times 2 = 10$$

$$2 + 2 + 2 + 2 + 2 = 10$$

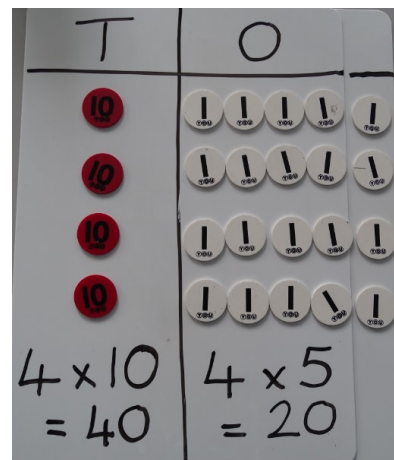
$$5 + 5 = 10$$

Partition to multiply (use numicon, Dienes, Cuisenaire rods)

$$4 \times 15$$



Children to represent the concrete manipulatives in a picture



Children to be encouraged to show the steps they have taken

$$\begin{array}{r} 4 \times 15 \\ \swarrow \searrow \\ 10 \quad 5 \end{array}$$

$$10 \times 4 = 40$$

$$5 \times 4 = 20$$

$$40 + 20 = 60$$

Children to move to show partitioning steps in an expanded column method.

$$\begin{array}{r} T \\ 1 5 \\ \times \textcircled{4} \\ \hline 20 \\ + 40 \\ \hline 60 \end{array} \quad \begin{array}{l} 4 \times 5 \\ 4 \times 10 \end{array}$$

Concrete

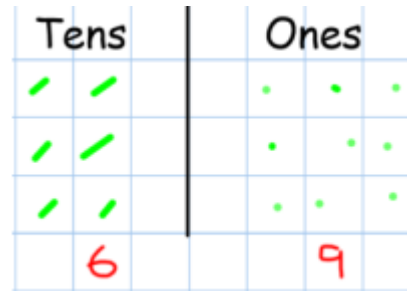
Formal column method with place value counters or base 10 (at the first stage no exchanging)
 3×23 .

Make 23, 3 times. See how many ones, then how many tens.



Pictorial

Children to represent the counters in a pictorial way



Abstract

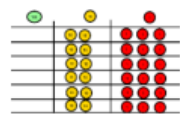
Children to record what it is they are doing to show understanding

$$\begin{array}{r}
 3 \times 23 \\
 \begin{array}{l} \diagup \\ \diagdown \end{array} \\
 20 \quad 3 \\
 3 \times 20 = 60 \\
 3 \times 3 = 9 \\
 60 + 9 = 69
 \end{array}$$

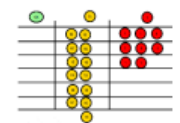
$$\begin{array}{r}
 23 \\
 \times 3 \\
 \hline
 69
 \end{array}$$

Formal column method with place value counters (children need this stage, initially, to understand how the column method works)

$$6 \times 23$$



Step 1: get 6 lots of 23



Step 2: 6×3 is 18. Can I make an exchange? Yes! Ten ones for one ten....

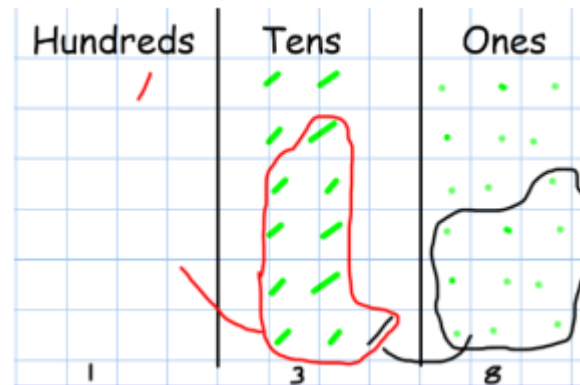


Step 3: 6×2 tens and my extra ten is 13 tens. Can I make an exchange? Yes! Ten tens for one hundred...



Step 4- what do I have I each column?

Children to represent the counters/Dienes, pictorially e.g. the image below.



The aim is to get to the formal method but the children need to understand how it works.

$$\begin{array}{r}
 6 \times 23 = \\
 23 \\
 \times 6 \\
 \hline
 138 \\
 \hline
 1 \quad 1
 \end{array}$$